

## 15. WETTING AND SPREADING

$$\gamma_{sg} = \gamma_{sl} + \gamma_{lg} \cos \theta$$

$$W_c = 2 \gamma_{lg}$$

$$W_a = \gamma_{lg} + \gamma_{sg} - \gamma_{ls} = \gamma_{lg} (1 + \cos \theta)$$

$$S_{l/s} = W_a - W_c = \gamma_{sg} - \gamma_{lg} - \gamma_{ls}$$

### Problem 15-01 Young equation, wetting angle

A small amount of liquid of density  $0.779 \text{ g cm}^{-3}$  and surface tension  $28.4 \text{ mN m}^{-1}$ , placed on the surface of plane alumina plate forms a sessile drop with a contact angle  $\theta = 115^\circ$ .

(a) Sketch the shape of the drop with the interfacial tensions and contact angle

(b) The interfacial tension between the liquid and the solid surface is  $38 \text{ mN m}^{-1}$ . Calculate the surface energy of the solid surface.



### Problem 15-02 Spreading coefficient, cohesion work

A drop of liquid placed on the plane surface of paraffin exhibits the contact angle  $128^\circ$ . The surface tension of the liquid is  $28.5 \text{ mN m}^{-1}$ . Calculate the cohesion work and Harkins spreading coefficient. [ $W_c = 43 \text{ mJ m}^{-2}$ ,  $S_{l/s} = 47.5 \text{ mJ m}^{-2}$ ]

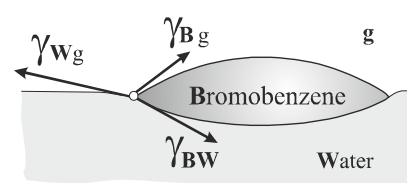
### Problem 15-03 Spreading of a liquid on solid surface

A small amount of liquid was placed on a plane surface of a solid, the surface energy of which was  $48.5 \text{ mJ m}^{-2}$ . How will it behave? Will it spread? The interfacial tension liquid-solid surface has the value of  $18.3 \text{ mN m}^{-1}$ . The surface tension of the liquid has been determined by the capillary rise method: in the vertical capillary of inner diameter  $0.16 \text{ mm}$  the elevation of the liquid of  $5.7 \text{ cm}$  was measured. The liquid density is  $0.912 \text{ g cm}^{-3}$  and the studied liquid completely wets the walls of the capillary.

$$[\gamma_{sg} > \gamma_{sl} + \gamma_{lg}; S_{l/s} = 9.8 > 0, \cos \theta > 1 - \text{liquid spreads } (\gamma_{lg} = 20.4 \text{ mN m}^{-1})]$$

### Problem 15-04 Spreading of a liquid on liquid surface

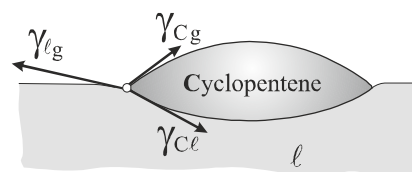
The surface tension of bromobenzene (B) at the temperature of  $20^\circ\text{C}$  is  $35 \text{ mN m}^{-1}$  and its density has the value of  $1.495 \text{ g cm}^{-3}$ , the surface tension and density of water (W) are  $72.75 \text{ mN m}^{-1}$  and  $0.9982 \text{ g cm}^{-3}$ , respectively. Interfacial tension between water and bromobenzene is  $39 \text{ mN m}^{-1}$ . Will a small amount of bromobenzene spread on the water surface or it will take the form of a lens?



$$[S_{B/W} = \gamma_{Wg} - \gamma_{Bg} - \gamma_{BW} = -1.25 \text{ mN m}^{-1} < 0 \Rightarrow \text{bromobenzene does not spread}]$$

### Problem 15-05 Spreading of a liquid on liquid surface

Estimate what is the minimal value of the interfacial tension between cyclopentene (C) and another liquid ( $\ell$ ), immiscible with cyclopentene, at which the cyclopentene would still spread on this liquid surface. The surface tension of the liquid was measured by the capillary rise method: at the temperature of  $20^\circ\text{C}$  the level of the studied liquid in the glass capillary of inner diameter of  $0.8 \text{ mm}$  climbed to the height of  $2.5 \text{ cm}$  above the horizontal level of the liquid in the wide beaker. The liquid density is  $1.06 \text{ g cm}^{-3}$  and it wets the material of the capillary completely. The density of cyclopentene is  $0.762 \text{ g cm}^{-3}$ , molar mass  $68 \text{ g mol}^{-1}$ , and its surface tension  $21.6 \text{ mN m}^{-1}$ .



$$[\gamma_{C/\ell} < 30.4 \text{ mN m}^{-1} (\gamma_{lg} = 52 \text{ mN m}^{-1})]$$