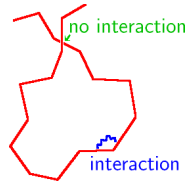


## Polymer solutions

1/16  
co/13

### Model of the ideal chain:

- beads are connected by flexible bonds/angles/torsions
- beads far enough do not interact (by solvent-mediated effective interaction)
- = random walk = trajectory of Brownian motion



Brownian motion:  $\langle r^2 \rangle = 6D$ , time corresponds to the number of beads  $N$   
 $\Rightarrow$  coil size  $\propto N^{1/2}$

### Better models:

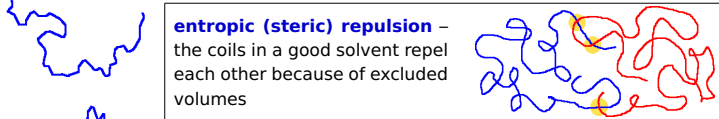
- repulsive forces  $\rightarrow$  excluded volume (beads do not overlap)
- attractive forces  $\rightarrow$  "negative excluded volume" (beads are "sticky")

## Polymer solutions II

2/16  
co/13

**good solvent** – (lyophilic polymer), beads effectively repel each other, the chain partly unwinds = self-avoiding random walk coil size  $\propto N^{1.7}$

**entropic (steric) repulsion** – the coils in a good solvent repel each other because of excluded volumes



**theta-solvent** – beads interact with the solvent in the same way as mutually (effectively repulsion = attraction)  $\approx$  ideal chain coil size  $\propto N^{1/2}$

**bad solvent** – (lyophobic polymer), chain shrinks and packs to a smaller volume, some solvent between chains coil size  $\propto N^{1/3}$

**non-solvent** – no solvent between chains, size  $\propto N^{1/3}$

## Electroosmosis

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co/13

Smoluchowski (also Helmholtz-Smoluchowski) equation:

$$v = \frac{\epsilon \zeta \mathcal{E}}{\eta} \quad \text{or using mobility: } u = \frac{\epsilon \zeta}{\eta} \quad (1)$$

El. current across area  $A_0$ :  $A_0 I = A_0 \epsilon \kappa = A_0 \frac{U}{L} \kappa$  ( $\kappa$  = conductivity)

Volume flow:  $\frac{dV}{d\tau} = v A_0$

$$\frac{dV/d\tau}{I} = \frac{\epsilon \zeta}{\eta \kappa} \quad (2)$$

Eq. (1) also holds for electrophoresis with coefficient 2/3 provided that the particles are large enough and distant ( $\gg \lambda$ ). For small particles  $\rightarrow$  ionic conductivity,  $u \propto 1/\eta$ .

Eqs. (1) and (2) are used to measure the  $\zeta$  potential

Colloid stability requires  $|\zeta| > 40$  mV.

**Isoelectric point:** the concentration of ions or pH so that  $\zeta = 0$  ( $\approx$  a particle is not charged) – typical for polyelectrolytes (proteins with both  $-NH_2$  and  $-COOH$ ). Smallest repulsion – best folded

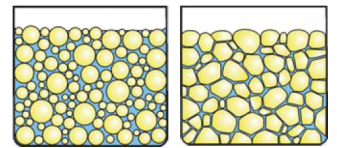
**Example.** Small cavities in a solution of soap move towards the anode

## Emulsions

6/16  
co/13

Types:

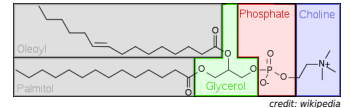
- O/W (oil-in-water): less polar liquid (oil) in a more polar liquid (water)
- W/O (water-in-oil)



Examples: milk, mayonnaise, cutting fluids (for metals)

Most properties given by the continuous phase (medium): el. conductivity, wetting, dissolution of dyes

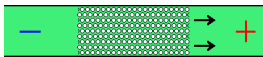
Concentrated emulsions must be stabilized by an **emulsifier** – surfactant, e.g., lecithin (phosphatidylcholine)



Instability: flocculation (aggregation – bound by elst. forces), coalescence (of droplets), creaming (sedimentation), Ostwald ripening

## Electrokinetic phenomena

[vlc show/hgheart.mov] 3/16  
co/13

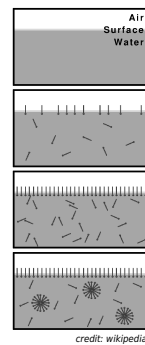


- electroosmosis – motion of an ionic solution through a porous material or capillary induced by an applied electric field (electroosmotic flow); if pressure is applied against: electroosmotic pressure
- reversed: flow of the solution produces an electroosmotic potential
- electrophoresis – motion of a colloid particle in an ionic solution induced by an applied electric field
- reversed: sedimentation potential or current

Different is the **electrocapillarity**, change of the surface tension with applied voltage (e.g., mercury)  
 movie: jchemed.chem.wisc.edu

## Micelles

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co/13

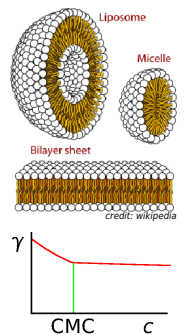


**Micelle** = usually spherical composed of a surfactant and stabilized:  
 – lyophilic interaction (w. the solvent)  
 – lyophobic interaction (inside)

**Creation:** solution  $\rightarrow$  microaggregation  $\xrightarrow{CMC}$  micelle  $\rightarrow$  cylindrical or lamellar micelles, liquid crystals, ...

CMC = **critical micelle concentration**: "Surface too crowded". Slope change on the curve  $\gamma$  vs.  $c$  (is not a phase transition – not abrupt)

**Inverse micelle** (butter)



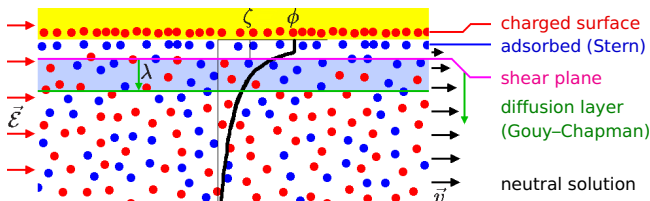
**Solubilization** – ability of micelles do absorb lyophobic substances

**Detergency** – washing

## Electroosmosis

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co/13

**Shear plane**, slipping plane = approximative plane dividing the moving liquid from the stationary liquid close to the surface



Surface charge =  $\sigma$ , el. field intensity =  $\mathcal{E}$ , viscosity =  $\eta$

$$\text{Tangent el. force per area: } \sigma \mathcal{E} = \eta \frac{v}{\lambda} \Rightarrow \text{velocity } v = \frac{\sigma \mathcal{E} \lambda}{\eta}$$

Double layer capacity (per area)  $C/A = \epsilon/\lambda$

$$\sigma = \frac{C}{A} \zeta = \frac{\epsilon}{\lambda} \zeta \Rightarrow v = \frac{\epsilon \mathcal{E}}{\eta} \zeta$$

potential at the shear plane =  $\zeta$  = **zeta-potential** = electrokinetic potential

## Phase transition classification

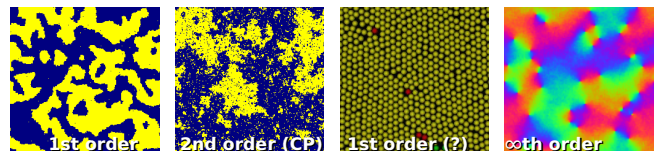
[showvid pic/harddisks.vid] + 8/16  
co/13

- 1st order: slope change of  $G$ , discontinuity in enthalpy, density (crystallization, vaporization, ...)
- 2nd order: Ehrenfest: discontinuity in enthalpy, density; higher derivatives modern: higher derivatives diverge ("continuous") (critical point [CP], Curie point, lambda-transition He)
- $\infty$ th order ("continuous"): e.g., Kosterlitz-Thouless (some 2D systems): all derivatives continuous ( $f(x) = \begin{cases} e^{-1/x} & \text{pro } x > 0 \\ 0 & \text{pro } x <= 0 \end{cases}$ )

Glass transition = viscosity  $> 10^{12}$  Pa s – not a phase transition

Micellization (at CMC) is not a phase transition

Micelle crystallization (to a lamellar/fibrillar phase) is 1st order phase transition



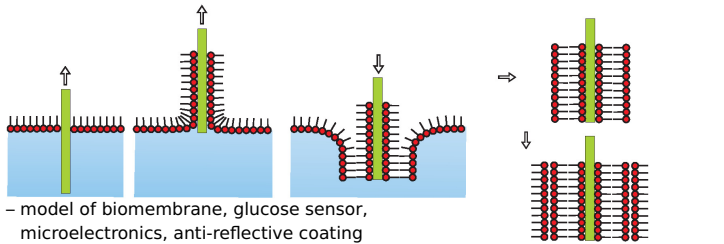
## Double layer

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col13

Two layers of a surfactant; cell membrane = phospholipid double layer ("glued" together by the hydrophobic ends, usually 2D liquid)

**vesicle** – liquid inside  
vacuoles, liposomes, transport vesicles...  
artificial liposomes: drug transport

**Langmuir-Blodgett films:** more (double) layers, usu. 2D crystal



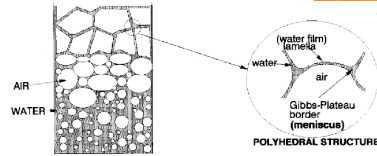
– model of biomembrane, glucose sensor, microelectronics, anti-reflective coating

## Foams

13/16  
col13

Gas in liquid

- wet foams (spherical cavities, "bubbles")
- dry foams (polyhedra, 12–14)
- Gibbs–Plateau channels
- Plateau rules (see lecture 10)



Stabilized by surfactants

destabilization: gravity, evaporation, Ostwald ripening, film rupture

Dry foams (styrofoam)

credits: <http://galerie.albumfotek.cz/krvavydedek/>, Kim&Kim

## Gels

10/16  
col13

Connected 3D network of the dispersed phase (and the medium), do not flow

Generally **lyogel**, in water **hydrogel**, (dried) **xerogel**

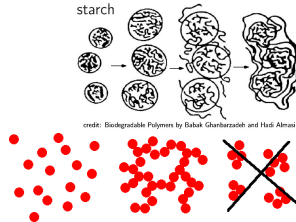
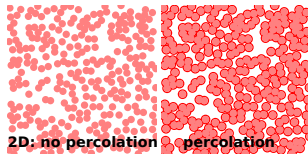
reversible gel: gel  $\xrightleftharpoons[\text{swelling}]{\text{drying}}$  xerogel

sometimes reversibility refers to the sol  $\rightleftharpoons$  gel process

- gelatinization of macromolecule solutions:
  - cross-linking by chemical bonds
  - association (vdW, H-bonds)
  - crystalline links
  - geometric (entanglement)

- destabilization of (lyophobic) sols with linking (not coagulation)

older gels: syneresis (swelling of the structure – yoghurt)



## Foams: Plateau rules

14/16  
col13

By Joseph Plateau (1801–1883)\*

- smooth surfaces
- constant curvature  $1/R_x + 1/R_y$
- surfaces meet at angle  $120^\circ$
- channels meet at tetrahedral angles  $\arccos(-1/3) = 109.47^\circ$



\*known also for "phenakistiscope" and Plateau–Rayleigh instability

## Gels II

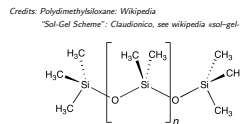
11/16  
col13

**Mechanical properties:**

- elasticity (a few covalent links)
- thixotropy (reversible weak links)

**Hydrogels:**

- contact lenses (polyacrylamides, "silicone" – oxygen-permeable)
- diapers (sodium polyacrylate,  $[-CH_2-CH(COONa)-]_n$ )
- biomaterials – silicon implants, scaffolding for tissue growth



## Aerosols

15/16  
col13

Liquid dispersion: fog (10 nm – 10  $\mu$ m)

Solid dispersion: smoke (to 10  $\mu$ m), dust (above 10  $\mu$ m)

**Destabilization:**

- sedimentation (stabilized by sun radiation: heated)
- coagulation (stabilized by el. charge)

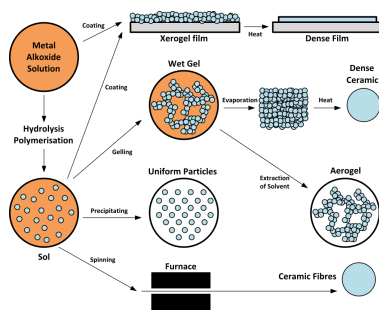
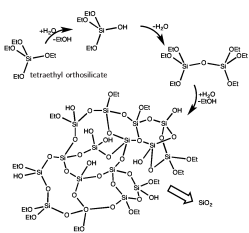
**Particle charge:** (electro)spraying (nozzle, wind+sea), ionization by UV, grinding of ionic crystals

Aerosol of flammable dust may explode (flour, coal)

## Gels III

12/16  
col13

**Sol-gel process:** Synthesis of colloid particles followed by gelatinization and production of solid materials (ceramics, layers, fibers)



**Aerogel** = xerogel with a very low density (supercritical drying), silica gel to  $1.9 \text{ g dm}^{-3}$ ; alumina; aerographite  $0.18 \text{ g dm}^{-3}$  – ultimate tensile strength 1 kPa

**Use:** insulation, adsorbent, Cherenkov detector

## Atmospheric aerosols

16/16  
col13

**troposphere**

- clouds  
nucleation of droplets around dust, ions, salts ( $(\text{NH}_4)_2\text{SO}_4$  most typical)  
polarizable anions at surface of droplets
- solid aerosols  
most stable  $\approx 300 \text{ nm}$ :  
– smaller particles diffuse fast and get adsorbed  
– larger particles sediment  
particles  $< 10 \mu\text{m}$  (PM10, = aerodynamic diameter) are not filtered in the nose, may penetrate to alveoli and (smaller ones) to the blood
- smog ( $<$  smoke and fog):  
– London (reduction) type (smoke, fog,  $\text{SO}_2$ ); vog = volcanic smog  
– photochemical (ox.) smog (L.A.):  $\text{NO}_2 + \text{VOC} + h\nu \rightarrow \text{O}_3 + \dots$

PM = Particulate Matter

VOC = Volatile Organic Compound

**stratosphere**

- soot (does not sediment because heated)
  - volcanic ash,  $\text{SO}_2 \rightarrow \text{SO}_4^{2-}$  ( $\rightarrow$  cooling)
- nuclear winter (soot), volcanic winter (ash,  $\text{SO}_x$ )