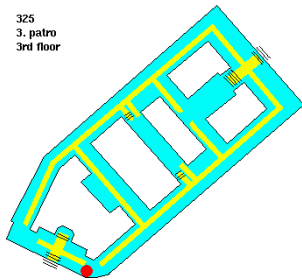


## Info

1/23  
s00/3

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Google: Kolafa Molecular modeling and simulation  
Kolafa Molekulární modelování a simulace

## Molecular simulations

6/23  
s00/3

- molecular dynamics (MD)
  - time development of a system composed of many molecules
  - instantaneous forces acting on atoms cause their motion
- Monte Carlo (MC); more precisely: Metropolis method and its variants
  - a sequence of configurations of the system is generated using random numbers
  - an attempt is made to move a molecule (randomly with a certain distribution)
  - this trial move is accepted or rejected so that its probability is the same as in reality
- kinetic Monte Carlo
  - the simulated process is divided into elementary events (e.g., adsorption of an atom on a growing crystal, catalytic reaction)
  - the event to happen is chosen according to a known probability
- quantum simulations – MD, MC
- Las Vegas algorithms – deterministic result (random pivot, search for minimum)

## Elements of modeling

2/23  
s00/3

- ? elementary particles + gravity, GUT, dark energy, ...
- known elementary particles: Standard model, atomic nuclei, ...
- Nuclei + electrons + photons: QED, accurate spectroscopy
- Nuclei + electrons: Schrödinger equation – small molecules, spectra, gas-phase equilibria, chemical kinetic, photochemistry ...
- Atoms\* – classical (or quantum) atomistic modeling
- Coarsened-grained models: meso/nanoscale element = polyatomic group (surfactant = head + tail, polymer = [bead]<sub>n</sub> ...)
- Microscopic scale (dispersions, granular materials)
- Continuum: partial differential equations – heat, weather models, neutrons in A-bomb, statics in civil engineering
- gravity: spacetime – black holes, gravitational waves

multiscale modeling: QM/MM (enzymes etc.) ...

\*optionally: auxiliary interaction centers (sites), bigger groups (-CH<sub>3</sub>)

## What can be studied

7/23  
s00/3

- Liquids:
  - how structure affects properties (anomalies of water), solutions
  - phase equilibria, solubility
  - surfaces, interfaces, surfactants
- Solids:
  - crystal structure, materials (defects)
  - adsorption (zeolites)
- Biochemistry:
  - proteins, nucleic acids, ion channels, lipid membranes
- Nanoobjects:
  - micelles, polymers, self-assembly (coarse-grained models, lattices)
- Similar methods can be used for:
  - granular materials, optimization, spreading of epidemics, active matter, agent-based models, evo-devo (evolutionary developmental biology) ...

## Potential Energy Surface (PES)

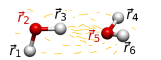
[show/SPCEdimer.sh] 3/23  
s00/3

Nuclei are much heavier than electrons ⇒ electron motion is much faster (Born-Oppenheimer approximation)

Potential energy surface (PES):

energy as a function of positions of all nuclei

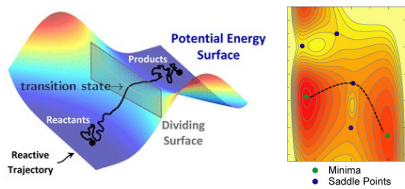
$$E_{\text{pot}}(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)$$



### Chemical example:

reaction coordinate

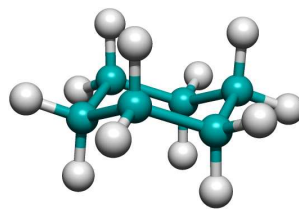
A reaction proceeds over (near to) a saddle point (transition state)



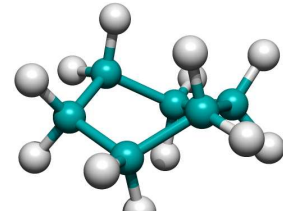
credits: <http://www.ucl.ac.uk/~ucecmst/publications.html>, <http://theory.cm.utexas.edu/henkelman/research.html>

## Structure optimization (example of molecular mechanics)

[uvodsim/blend.sh] 8/23  
s00/3



chair  
experiment: 28 kJ/mol  
model: 26 kJ/mol



twist (skew) boat  
experiment: 45 kJ/mol  
model: 53 kJ/mol

## How to obtain PES?

4/23  
s00/3

- from quantum calculations (Schrödinger equation: *ab initio*, DFT)
- approximated by a formula ("force field", "potential", "model", ...)  
**force field**:  $E_{\text{pot}}$  = sum of many terms  
term = function form + parameters for atoms/groups
- combination: QM/MM methods (quantum mechanics/molecular mechanics)

## PES and modeling in chemistry

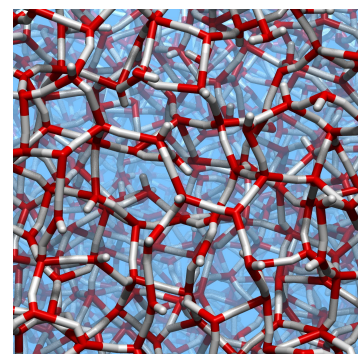
- using classical mechanics:
  - static calculations: minimum of energy, potential around a molecule
  - time development of system (molecular dynamics, MD);  
with *ab initio* PES = AIMD (demanding!)  
thermodynamic variables by sampling (Monte Carlo, MC)
- using quantum mechanics to nuclei:
  - path integral methods (PI MC, PI MD); with AIMD extremely demanding
  - classical mechanics + quantum corrections

combination force field + classical mechanics = "molecular mechanics" (MM); strictly speaking does not include MC and MD

## Liquid water (example of equilibrium molecular dynamics)

[water/liquidwater.sh] 9/23  
s00/3

- 10000 molecules
- 300 K
- periodic in x, y
- adhesive pad
- nonadhesive lid



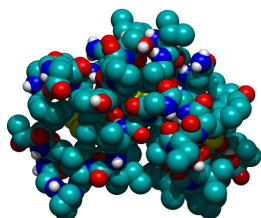
More movies: <https://vesmir.cz/cz/on-line-clanky/2014/07/struktura-anomalie-vody.html>

## Molecular mechanics: static approach

5/23  
s00/3

We use PES, usually described by a force field

- Energy minimization ( $T = 0$ )  
"molecular mechanics", "structure optimization"
- Refinement – more accurate structure (from diffraction data)
- Biochemistry: molecular shape (lock and key), hydrophilic/hydrophobic
- QSAR (Quantitative Structure-Activity Relationship) descriptors

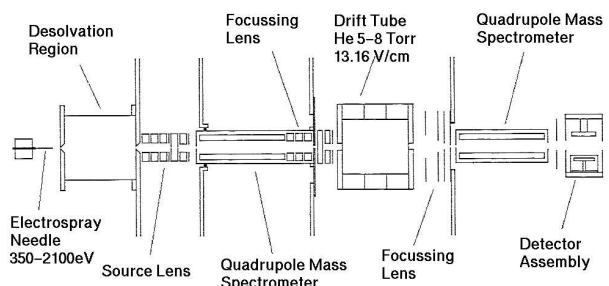


... but what about motion?

## Electrospray of Cytochrome C

[uvodsim/cytox.sh] 10/23  
s00/3

- Electrospray: spray of charged aerosol
- Cross section is determined



Yi Mao, J. Woenckhaus, J. Kolafa, M. A. Ratner, M. F. Jarrold: *J. Am. Chem. Soc.* **121**, 2712-2721 (1999)

## SIMOLANT

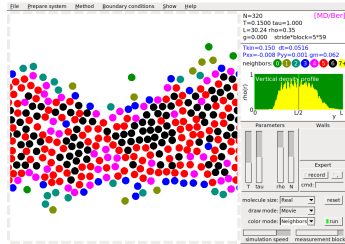
[simolant]11/23  
s00/3

### Features:

- 2D "atoms" with a Lennard-Jones type potential (8-4)
- repulsive/attractive walls, gravity
- MC and MD
- constant energy and thermostat

### Phenomena:

- condensation of vapor
- freezing of a droplet
- crystal defects
- capillary action
- gas in a gravitational field
- vapor-liquid equilibrium
- nucleation



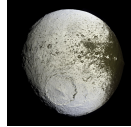
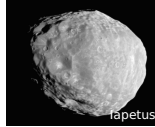
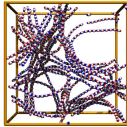
Install SIMOLANT: <http://old.vscht.cz/fch/software/simolant/index-en.html>

## Self-assembly (primitive example)

[show/janus.sh]12/23  
s00/3

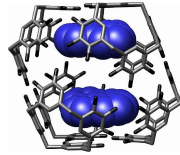
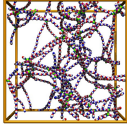
**Supramolecular chemistry:** assembling molecules using noncovalent forces (van der Waals, hydrogen bonds) to higher structural elements

- Show: bivalent particles in a solution ≈ "Janus particles"



credit: wikipedia, www.nasa.gov/mission\_pages/cassini

- Show: + tetravalent particles

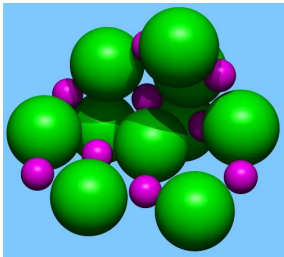


credit: Atwood et al., Science 309, 2037 (2005)

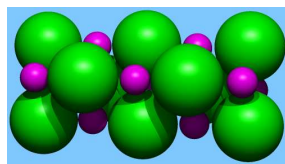
## How to get energy minimum (simulated annealing)

[uvodsim/min.sh]13/23  
s00/3

Minimum energy of (a model of) Na<sub>10</sub>Cl<sub>10</sub> cluster



fast cooling (quenching)



slow cooling (annealing)

## Optimization by simulated annealing

[uvodsim/salesman.sh 100]14/23  
s00/3

We are looking for the **global minimum** of function  $U(A_i)$  (with many local minima)

- Configuration changes  $A_i \rightarrow A_j$
- Metropolis MC simulation while decreasing "temperature"  $T$

**Example:** Traveling salesman problem

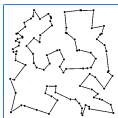
- 100 cities randomly in square  $1 \times 1$
- Configuration = sequence of cities
- $U$  = path length
- Configuration change = interchange of 2 randomly chosen cities

for me (uvodsim/salesman.sh):  
- random start  
- numerical results in the console

"greedy"  
(Metropolis  $T=0$ )  
 $l = 8.5778$



simulated  
annealing  
 $l = 7.6663$



genetic  
algorithm  
 $l = 8.1817$



## Genetic algorithms (evolutionary programming)

+ 15/23  
s00/3

The function to maximize is called here "fitness"

- configuration  $\rightarrow$  individual  $\rightarrow$  genom = chromosome = list of alleles ("column of numbers")
- initial (e.g., random) population
- next generation:
  - kill the least fit individuals
  - copying (parthenogenesis) with a mutation
  - breeding from two parents with crossover

Numbers are coded by a Gray code (consecutive integers differ by one bit)

### Application:

- logistics, economy, control of processes
- biochemistry - protein folding
- electronics - circuit design, antenna shape
- algorithm design

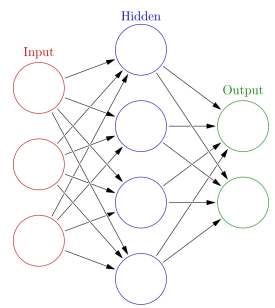
0 0000  
1 0001  
2 0011  
3 0010  
4 0110  
5 0111  
6 0101  
7 0100  
8 1100  
9 1101  
10 1111  
11 1110  
12 1010  
13 1011  
14 1001  
15 1000

## Artificial neural networks

+ 16/23  
s00/3

- several layers
- discrete or continuous signal
- usually  $\rightarrow$ , rarely with feedback
- nonlinear activation function (sigmoid)
- weights for input mixing are adjustable

**learning** = determining the weights using a training set (optimization)

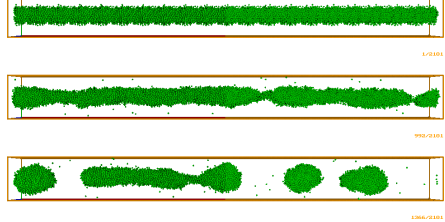


## Self-assembly (primitive example)

[./simul/rayleigh/show.sh]17/23  
s00/3

## (Plateau-)Rayleigh instability

A stream of water splits into droplets. Instability for  $kr < 1$  (for perturbation  $\propto \sin(kz)$ ), max. instability for  $kr = \ln 2$ .

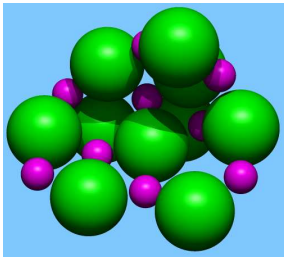


NB: " $\propto$ " = "is proportional to"

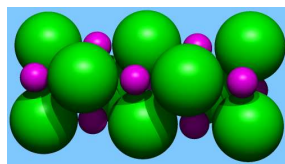
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[uvodsim/min.sh]13/23  
s00/3

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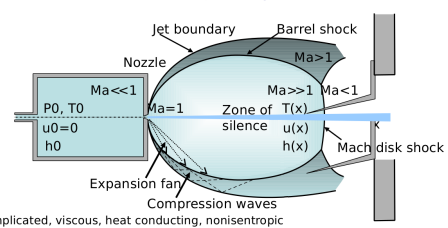
## Nucleation at supersonic expansion

[show/supexp.sh]18/23  
s00/3

Water vapor (about 150 °C and 5 bar) expands through a small (100 μm) nozzle to a vacuum. It cools adiabatically below freezing point.

**Motivation:** stratospheric physical chemistry.

### Free Jet Expansion



complicated, viscous, heat conducting, nonisotropic

credit: M. Farnik

**Question:** what is the shape and structure of ice clusters?

J. Klíma, J. Kolafa: *J. Chem. Theory Comput.* **14**, 2332-2340 (2018)

## Optimization by simulated annealing

[uvodsim/salesman.sh 100]14/23  
s00/3

We are looking for the **global minimum** of function  $U(A_i)$  (with many local minima)

- Configuration changes  $A_i \rightarrow A_j$
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**Example:** Traveling salesman problem

- 100 cities randomly in square  $1 \times 1$
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for me (uvodsim/salesman.sh):  
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annealing  
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algorithm  
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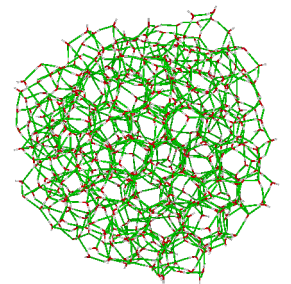


## Melting of nanoparticles

[show/kroupa.sh]19/23  
s00/3

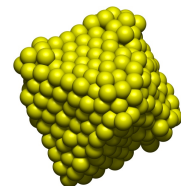
### Ice

- hail of 600 water molecules (ice Ih)
- gradual heating
- simulation time = 5 ns
- this model of water melts at 250 K



### Gold

- nanocrystal of 489 gold atoms
- gradual heating
- simulation time = 77 ps



the melting point  
of nanoparticles  
is lower than in the bulk

## Genetic algorithms (evolutionary programming)

+ 15/23  
s00/3

The function to maximize is called here "fitness"

- configuration  $\rightarrow$  individual  $\rightarrow$  genom = chromosome = list of alleles ("column of numbers")
- initial (e.g., random) population
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  - kill the least fit individuals
  - copying (parthenogenesis) with a mutation
  - breeding from two parents with crossover

Numbers are coded by a Gray code (consecutive integers differ by one bit)

### Application:

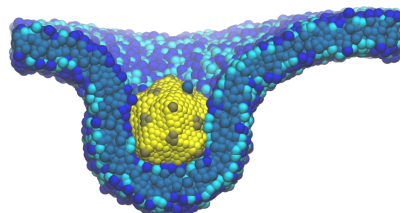
- logistics, economy, control of processes
- biochemistry - protein folding
- electronics - circuit design, antenna shape
- algorithm design

0 0000  
1 0001  
2 0011  
3 0010  
4 0110  
5 0111  
6 0101  
7 0100  
8 1100  
9 1101  
10 1111  
11 1110  
12 1010  
13 1011  
14 1001  
15 1000

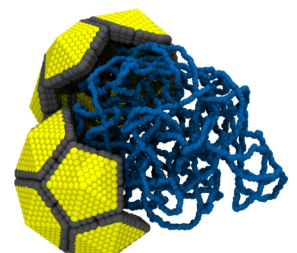
## Coarse-grained simulations

[vacha/vacha.sh]20/23  
s00/3

- Coarse-grained model, Langevin thermostat (random forces)
- Water not shown



endocytosis



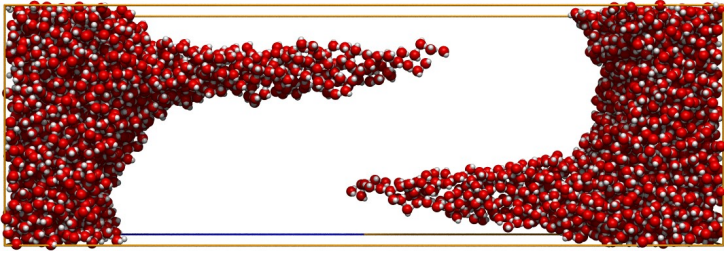
release of RNA from the capsid

Courtesy: © Robert Vácha (CEITEC)

## Electrospinning

[../simul/electrospinning/showcone.sh] 21/23  
s00/3

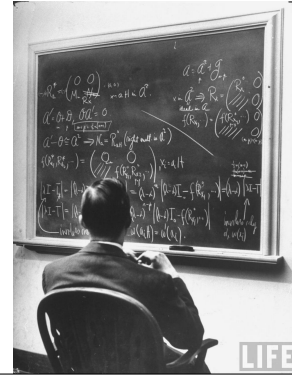
- 5000 SPC/E water molecules, field 1.5 V/nm, simulation time 135 ps
- electrospinning starts by the "Taylor cone"
- the tip elongates and produces a jet stabilized by electric field



Jan Jirsák, Filip Moučka, Ivo Nezbeda: *Ind. Eng. Chem. Res.* **53**, 8257–8264 (2014)

## End of introduction – real lecture ahead...

[showvid /home/jiri/macsimus/ray/dogrun/dogrun.vid] 23/23  
s00/3

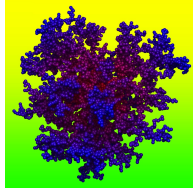


## Dendrimers by diffusion-limited aggregation

[/home/jiri/macsimus/show/dendrimer -n500] 22/23  
s00/3

### Fractals:

- Trajectory of Brownian motion = random walk = linear polymer in  $\theta$ -solvent:  $D = 2$
- Self-avoiding random walk = linear polymer in good solvent (in 3D):  $D = 1.7$
- Dendrimer in 2D:  $D = 1.7$
- Dendrimer in 3D:  $D = 2.5$
- Broccoli:  $D = 2.66$
- Lung surface:  $D = 2.97$



copper electrodeposition →

credit: Wikipedia

