

Aplikační příklad 4

Apl. příklad 4: Mějme rovnici popisující neizotermní vnitřní difuzi v částici katalyzátoru tvaru desky

$$\frac{\partial^2 y}{\partial x^2} = \phi^2 y e^{\frac{\alpha \beta (1-y)}{1+\beta(1-y)}},$$

$$\frac{\partial y}{\partial x}(0) = 0, \quad y(1) = 1.$$

Použijte parametry $\alpha=20$, $\beta=0.1$, $\phi=1$.

Definice parametrů diferenciální rovnice

```
 $\alpha = 20;$   
 $\beta = 0.1;$   
 $\phi = 1;$ 
```

Definice pravé strany diferenciální rovnice

```
f[x_, y1_, y2_] =  $\phi^2 y1 \text{Exp}[\frac{\alpha \beta (1 - y1)}{1 + \beta (1 - y1)}]$ ;
```

Parametry programu

```
a = 0.0;  
b = 1.0;  
 $\alpha 1 = 0;$   
 $\alpha 2 = 1;$   
 $\beta 1 = 1;$   
 $\beta 2 = 0;$   
 $\gamma 1 = 0;$   
 $\gamma 2 = 1;$   
 $\epsilon = 0.000001;$   
n = 20;  
y0 = Table[0.5, {i, 1, n + 1}];  
y0[[1]] = 1.0;  
y0[[n + 1]] = 1.0;
```

```

yres = DESite2[n, f, a, b,  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$ ,  $\beta_2$ ,  $\gamma_1$ ,  $\gamma_2$ ,  $\epsilon$ , y0, 10];
iterace = 0

y={0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5,
  0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 0.5, 1.}

iterace = 1      s = 0.346106

y={0.356569, 0.358146, 0.362878, 0.370767, 0.381817, 0.396037,
  0.413434, 0.434018, 0.457802, 0.484801, 0.515031, 0.548509, 0.585257,
  0.625295, 0.66865, 0.715345, 0.76541, 0.818875, 0.875772, 0.936134, 1.}

iterace = 2      s = 0.0221961

y={0.374136, 0.375659, 0.380226, 0.387852, 0.398553, 0.412356,
  0.42929, 0.449386, 0.472674, 0.499182, 0.528931, 0.561933, 0.598188,
  0.637682, 0.680384, 0.726248, 0.775205, 0.827171, 0.882042, 0.939697, 1.}

iterace = 3      s = 0.000369655

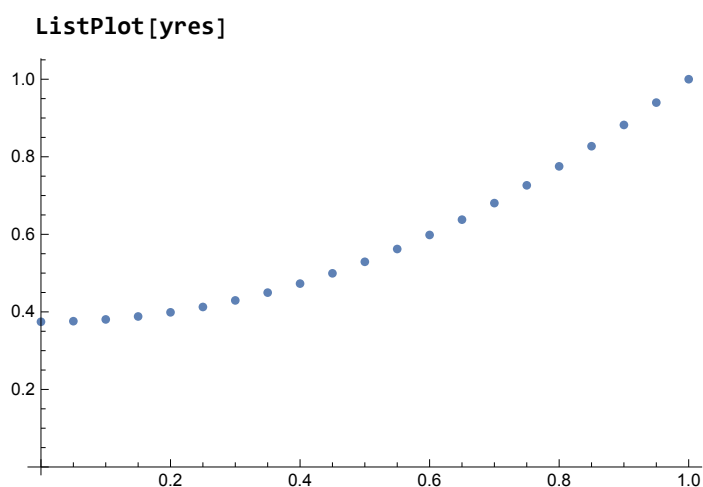
y={0.374465, 0.375986, 0.38055, 0.38817, 0.398863, 0.412657,
  0.429579, 0.449661, 0.472934, 0.499426, 0.529157, 0.562139, 0.598374,
  0.637846, 0.680527, 0.726367, 0.775301, 0.827244, 0.88209, 0.939721, 1.}

iterace = 4      s = 1.15361 $\times 10^{-7}$ 

y={0.374465, 0.375986, 0.380551, 0.38817, 0.398864, 0.412657,
  0.429579, 0.449661, 0.472934, 0.499426, 0.529157, 0.562139, 0.598374,
  0.637846, 0.680527, 0.726367, 0.775301, 0.827244, 0.88209, 0.939721, 1.}

```

Graf řešení $y(x)$



Tabulka řešení $y(x)$

MatrixForm[yres]

$$\begin{pmatrix} 0. & 0.374465 \\ 0.05 & 0.375986 \\ 0.1 & 0.380551 \\ 0.15 & 0.38817 \\ 0.2 & 0.398864 \\ 0.25 & 0.412657 \\ 0.3 & 0.429579 \\ 0.35 & 0.449661 \\ 0.4 & 0.472934 \\ 0.45 & 0.499426 \\ 0.5 & 0.529157 \\ 0.55 & 0.562139 \\ 0.6 & 0.598374 \\ 0.65 & 0.637846 \\ 0.7 & 0.680527 \\ 0.75 & 0.726367 \\ 0.8 & 0.775301 \\ 0.85 & 0.827244 \\ 0.9 & 0.88209 \\ 0.95 & 0.939721 \\ 1. & 1. \end{pmatrix}$$