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Get[FileNameJoin[{NotebookDirectory[], "DeSite.wl"}]]
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Aplikační příklad 6

Apl. příklad 6: Jednoduchý model chování sloupce plasmy stlačované zářením odvodil Troesch ve tvaru nelineární okrajové úlohy

$$\frac{\partial^2 y}{\partial x^2} = \alpha \sinh(\alpha y) ,$$

$$y(0) = 0, \quad y(1) = 1.$$

Použijte parametry $\alpha = 0.8; 1; 2; 5; 10; 20$.

$\alpha = 0.8$

Definice parametrů diferenciální rovnice

```
 $\alpha = 0.8;$ 
```

Definice pravé strany diferenciální rovnice

```
f[x_, y1_, y2_] =  $\alpha$  Sinh[ $\alpha$  y1];
```

Parametry programu DESite2

```
a = 0.0;
```

```
b = 1.0;
```

```
 $\alpha 1 = 1;$ 
```

```
 $\alpha 2 = 1;$ 
```

```
 $\beta 1 = 0;$ 
```

```
 $\beta 2 = 0;$ 
```

```
 $\gamma 1 = 0;$ 
```

```
 $\gamma 2 = 1;$ 
```

```
 $\epsilon = 0.000001;$ 
```

```
n = 20;
```

```
y0 = Table[0.05 * (i - 1), {i, 1, n + 1}];
```

```
yres = DESite2[n, f, a, b,  $\alpha 1$ ,  $\alpha 2$ ,  $\beta 1$ ,  $\beta 2$ ,  $\gamma 1$ ,  $\gamma 2$ ,  $\epsilon$ , y0, 10];
```

```
iterace = 0
```

```
y={0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35,  
0.4, 0.45, 0.5, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, 1.}
```

```
iterace = 1      s = 0.0479017
```

```
y={0., 0.0449207, 0.0899133, 0.13505, 0.180403, 0.226046,  
0.272052, 0.318497, 0.365456, 0.413009, 0.461234, 0.510214, 0.560033,  
0.610777, 0.662537, 0.715407, 0.769485, 0.824873, 0.881679, 0.940014, 1.}
```

```
iterace = 2      s = 0.0000179775
```

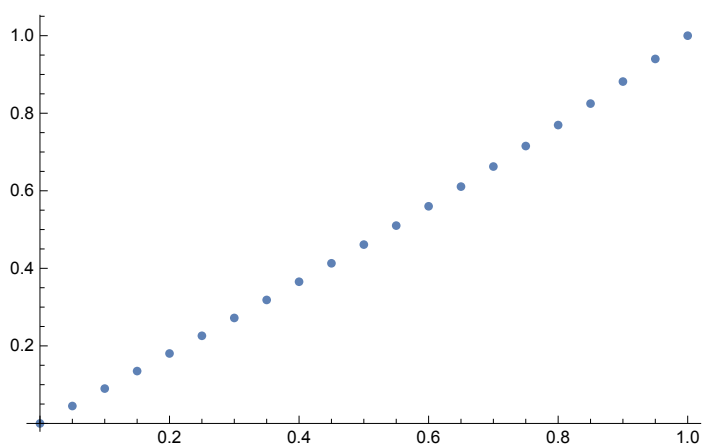
```
y={0., 0.044919, 0.08991, 0.135045, 0.180396, 0.226037,  
0.272042, 0.318485, 0.365444, 0.412995, 0.46122, 0.510199, 0.560018,  
0.610762, 0.662524, 0.715395, 0.769475, 0.824865, 0.881673, 0.940012, 1.}
```

```
iterace = 3      s = 2.26586  $\times 10^{-12}$ 
```

```
y={0., 0.044919, 0.08991, 0.135045, 0.180396, 0.226037,  
0.272042, 0.318485, 0.365444, 0.412995, 0.46122, 0.510199, 0.560018,  
0.610762, 0.662524, 0.715395, 0.769475, 0.824865, 0.881673, 0.940012, 1.}
```

Graf řešení $y(x)$

ListPlot[yres]



Tabulka řešení $y(x)$

MatrixForm[yres]

$$\begin{pmatrix} 0. & 0. \\ 0.05 & 0.044919 \\ 0.1 & 0.08991 \\ 0.15 & 0.135045 \\ 0.2 & 0.180396 \\ 0.25 & 0.226037 \\ 0.3 & 0.272042 \\ 0.35 & 0.318485 \\ 0.4 & 0.365444 \\ 0.45 & 0.412995 \\ 0.5 & 0.46122 \\ 0.55 & 0.510199 \\ 0.6 & 0.560018 \\ 0.65 & 0.610762 \\ 0.7 & 0.662524 \\ 0.75 & 0.715395 \\ 0.8 & 0.769475 \\ 0.85 & 0.824865 \\ 0.9 & 0.881673 \\ 0.95 & 0.940012 \\ 1. & 1. \end{pmatrix}$$

$\alpha = 1.0$

Definice parametrů diferenciální rovnice

$\alpha = 1.0;$

Definice pravé strany diferenciální rovnice

$f[x_, y1_, y2_] = \alpha \sinh[\alpha y1];$

Parametry programu DESite2

```

a = 0.0;
b = 1.0;
α1 = 1;
α2 = 1;
β1 = 0;
β2 = 0;
γ1 = 0;
γ2 = 1;
ε = 0.000001;
n = 20;
y0 = Table[0.05 * (i - 1), {i, 1, n + 1}];

yres = DESite2[n, f, a, b, α1, α2, β1, β2, γ1, γ2, ε, y0, 10];

iterace = 0

y={0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35,
  0.4, 0.45, 0.5, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, 1.}

iterace = 1      s = 0.0735046

y={0., 0.0422899, 0.0846855, 0.127293, 0.17022, 0.213574,
  0.257465, 0.302007, 0.347314, 0.393506, 0.440705, 0.48904, 0.538645,
  0.589659, 0.642231, 0.696518, 0.752688, 0.81092, 0.871407, 0.934358, 1.}

iterace = 2      s = 0.000102554

y={0., 0.0422808, 0.0846672, 0.127266, 0.170183, 0.213528,
  0.257411, 0.301944, 0.347244, 0.39343, 0.440624, 0.488957, 0.538561,
  0.589577, 0.642154, 0.696449, 0.75263, 0.810875, 0.871376, 0.934343, 1.}

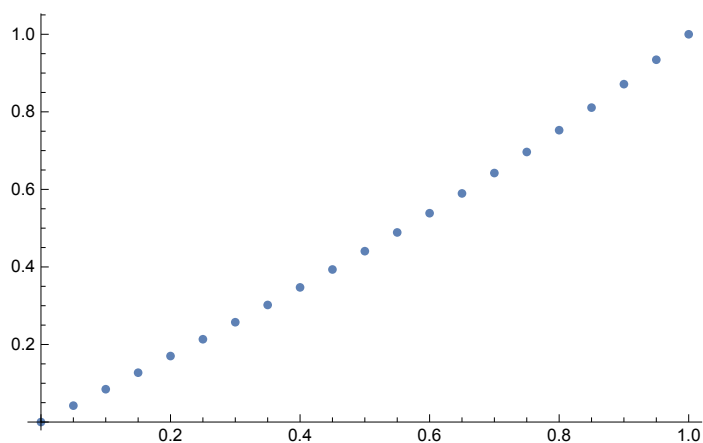
iterace = 3      s = 1.66341×10-10

y={0., 0.0422808, 0.0846672, 0.127266, 0.170183, 0.213528,
  0.257411, 0.301944, 0.347244, 0.39343, 0.440624, 0.488957, 0.538561,
  0.589577, 0.642154, 0.696449, 0.75263, 0.810875, 0.871376, 0.934343, 1.}

```

Graf řešení $y(x)$

ListPlot[yres]



Tabulka řešení $y(x)$

MatrixForm[yres]

$$\begin{pmatrix} 0. & 0. \\ 0.05 & 0.0422808 \\ 0.1 & 0.0846672 \\ 0.15 & 0.127266 \\ 0.2 & 0.170183 \\ 0.25 & 0.213528 \\ 0.3 & 0.257411 \\ 0.35 & 0.301944 \\ 0.4 & 0.347244 \\ 0.45 & 0.39343 \\ 0.5 & 0.440624 \\ 0.55 & 0.488957 \\ 0.6 & 0.538561 \\ 0.65 & 0.589577 \\ 0.7 & 0.642154 \\ 0.75 & 0.696449 \\ 0.8 & 0.75263 \\ 0.85 & 0.810875 \\ 0.9 & 0.871376 \\ 0.95 & 0.934343 \\ 1. & 1. \end{pmatrix}$$

$\alpha = 2.0$

Definice parametrů diferenciální rovnice

$\alpha = 2.0;$

Definice pravé strany diferenciální rovnice

$f[x_, y1_, y2_] = \alpha \text{Sinh}[\alpha y1];$

Parametry programu DESite2

$a = 0.0;$

$b = 1.0;$

$\alpha1 = 1;$

$\alpha2 = 1;$

$\beta1 = 0;$

$\beta2 = 0;$

$\gamma1 = 0;$

$\gamma2 = 1;$

$\epsilon = 0.000001;$

$n = 20;$

$y0 = \text{Table}[0.05 * (i - 1), \{i, 1, n + 1\}];$

```

yres = DESite2[n, f, a, b,  $\alpha$ 1,  $\alpha$ 2,  $\beta$ 1,  $\beta$ 2,  $\gamma$ 1,  $\gamma$ 2,  $\epsilon$ , y0, 10];
iterace = 0

y={0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35,
  0.4, 0.45, 0.5, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, 1.}

iterace = 1      s = 0.234818

y={0., 0.0270391, 0.0543483, 0.0821985, 0.110863, 0.140617,
  0.171743, 0.204532, 0.239288, 0.276335, 0.316026, 0.358754, 0.40497,
  0.455201, 0.510085, 0.570406, 0.637148, 0.711571, 0.795306, 0.8905, 1.}

iterace = 2      s = 0.0153383

y={0., 0.026006, 0.0522722, 0.0790621, 0.106646, 0.135304,
  0.165332, 0.197043, 0.230776, 0.266899, 0.305819, 0.347991, 0.39393,
  0.444227, 0.499574, 0.560788, 0.628861, 0.705016, 0.790799, 0.888225, 1.}

iterace = 3      s = 0.0000321098

y={0., 0.0260039, 0.052268, 0.0790558, 0.106637, 0.135293,
  0.165319, 0.197028, 0.230759, 0.26688, 0.305798, 0.347969, 0.393907,
  0.444204, 0.499552, 0.560768, 0.628844, 0.705002, 0.79079, 0.888221, 1.}

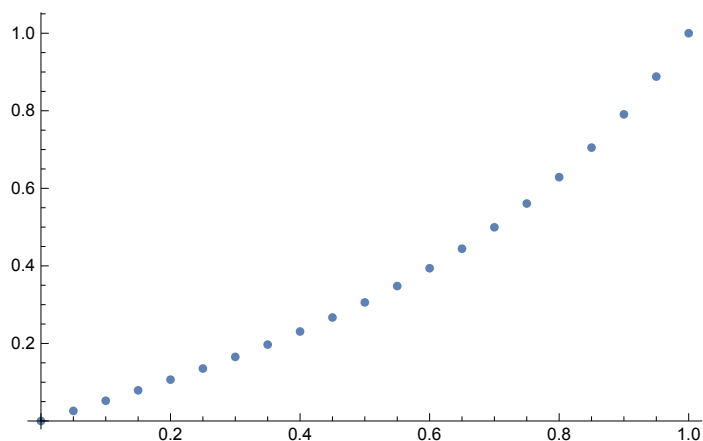
iterace = 4      s = 1.3601 $\times 10^{-10}$ 

y={0., 0.0260039, 0.052268, 0.0790558, 0.106637, 0.135293,
  0.165319, 0.197028, 0.230759, 0.26688, 0.305798, 0.347969, 0.393907,
  0.444204, 0.499552, 0.560768, 0.628844, 0.705002, 0.79079, 0.888221, 1.}

```

Graf řešení $y(x)$

ListPlot[yres]



Tabulka řešení $y(x)$

MatrixForm[yres]

$$\begin{pmatrix} 0. & 0. \\ 0.05 & 0.0260039 \\ 0.1 & 0.052268 \\ 0.15 & 0.0790558 \\ 0.2 & 0.106637 \\ 0.25 & 0.135293 \\ 0.3 & 0.165319 \\ 0.35 & 0.197028 \\ 0.4 & 0.230759 \\ 0.45 & 0.26688 \\ 0.5 & 0.305798 \\ 0.55 & 0.347969 \\ 0.6 & 0.393907 \\ 0.65 & 0.444204 \\ 0.7 & 0.499552 \\ 0.75 & 0.560768 \\ 0.8 & 0.628844 \\ 0.85 & 0.705002 \\ 0.9 & 0.79079 \\ 0.95 & 0.888221 \\ 1. & 1. \end{pmatrix}$$

$\alpha = 5.0$

Definice parametrů diferenciální rovnice

$\alpha = 5.0;$

Definice pravé strany diferenciální rovnice

$f[x_, y1_, y2_] = \alpha \sinh[\alpha y1];$

Parametry programu DESite2

$a = 0.0;$

$b = 1.0;$

$\alpha1 = 1;$

$\alpha2 = 1;$

$\beta1 = 0;$

$\beta2 = 0;$

$\gamma1 = 0;$

$\gamma2 = 1;$

$\epsilon = 0.000001;$

$n = 20;$

$y0 = \text{Table}[0.05 * (i - 1), \{i, 1, n + 1\}];$

```

yres = DESite2[n, f, a, b,  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$ ,  $\beta_2$ ,  $\gamma_1$ ,  $\gamma_2$ ,  $\epsilon$ , y0, 10];

iterace = 0

y={0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35,
  0.4, 0.45, 0.5, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, 1.}

iterace = 1      s = 0.274566

y={0., 0.018461, 0.0380466, 0.0597797, 0.0844912, 0.112753,
  0.14484, 0.18073, 0.220141, 0.262597, 0.307511, 0.354277, 0.402344,
  0.451264, 0.50072, 0.550545, 0.600799, 0.652188, 0.708194, 0.787115, 1.}

iterace = 2      s = 0.285183

y={0., 0.00721376, 0.014877, 0.0234582, 0.0334592, 0.045421,
  0.0599143, 0.0775107, 0.0987347, 0.124001, 0.153554, 0.187426, 0.225437,
  0.267268, 0.312617, 0.361519, 0.415026, 0.476901, 0.558463, 0.693904, 1.}

iterace = 3      s = 0.208217

y={0., 0.00314666, 0.00648993, 0.0102382, 0.0146241, 0.0199172,
  0.0264383, 0.0345735, 0.0447877, 0.0576355, 0.0737686, 0.0939399, 0.119015,
  0.150015, 0.18825, 0.235643, 0.295485, 0.374102, 0.484816, 0.65944, 1.}

iterace = 4      s = 0.0519403

y={0., 0.0024256, 0.00500281, 0.00789272, 0.011276, 0.0153643,
  0.0204135, 0.0267401, 0.0347413, 0.0449216, 0.0579263, 0.0745885, 0.0959949,
  0.123585, 0.159318, 0.205961, 0.267685, 0.351363, 0.469929, 0.653221, 1.}

iterace = 5      s = 0.00169866

y={0., 0.0024052, 0.00496072, 0.00782632, 0.0111812, 0.0152352,
  0.0202424, 0.0265169, 0.0344536, 0.0445543, 0.0574627, 0.0740121, 0.0952935,
  0.122759, 0.158387, 0.204982, 0.266753, 0.350596, 0.469431, 0.653016, 1.}

iterace = 6      s = 1.61546  $\times 10^{-6}$ 

y={0., 0.00240518, 0.00496068, 0.00782626, 0.0111811, 0.0152351,
  0.0202423, 0.0265167, 0.0344533, 0.0445539, 0.0574622, 0.0740116, 0.0952929,
  0.122758, 0.158386, 0.204981, 0.266752, 0.350596, 0.46943, 0.653015, 1.}

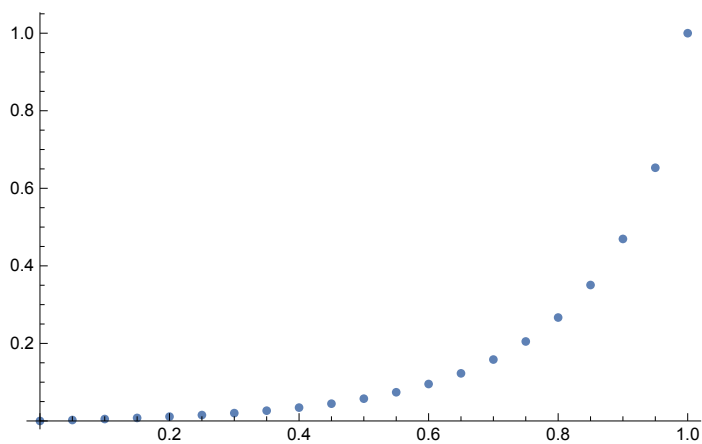
iterace = 7      s = 1.51195  $\times 10^{-12}$ 

y={0., 0.00240518, 0.00496068, 0.00782626, 0.0111811, 0.0152351,
  0.0202423, 0.0265167, 0.0344533, 0.0445539, 0.0574622, 0.0740116, 0.0952929,
  0.122758, 0.158386, 0.204981, 0.266752, 0.350596, 0.46943, 0.653015, 1.}

```

Graf řešení $y(x)$

ListPlot[yres, PlotRange → All]



Tabulka řešení $y(x)$

MatrixForm[yres]

0.	0.
0.05	0.00240518
0.1	0.00496068
0.15	0.00782626
0.2	0.0111811
0.25	0.0152351
0.3	0.0202423
0.35	0.0265167
0.4	0.0344533
0.45	0.0445539
0.5	0.0574622
0.55	0.0740116
0.6	0.0952929
0.65	0.122758
0.7	0.158386
0.75	0.204981
0.8	0.266752
0.85	0.350596
0.9	0.46943
0.95	0.653015
1.	1.

$\alpha = 10.0$

Definice parametrů diferenciální rovnice

$\alpha = 10.0;$

Definice pravé strany diferenciální rovnice

$f[x_, y1_, y2_] = \alpha \sinh[\alpha y1];$

Parametry programu DESite2

```

a = 0.0;
b = 1.0;
 $\alpha_1$  = 1;
 $\alpha_2$  = 1;
 $\beta_1$  = 0;
 $\beta_2$  = 0;
 $\gamma_1$  = 0;
 $\gamma_2$  = 1;
 $\epsilon$  = 0.000001;
n = 20;
y0 = Table[0.05 * (i - 1), {i, 1, n + 1}];

yres = DESite2[n, f, a, b,  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$ ,  $\beta_2$ ,  $\gamma_1$ ,  $\gamma_2$ ,  $\epsilon$ , y0, 12];

iterace = 0

y={0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35,
  0.4, 0.45, 0.5, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, 1.}

iterace = 1      s = 0.15274

y={0., 0.018906, 0.0420738, 0.0722755, 0.109999, 0.153744, 0.201177, 0.25033, 0.300092,
  0.350029, 0.40001, 0.450003, 0.500001, 0.55, 0.6, 0.65, 0.7, 0.75, 0.8, 0.85006, 1.}

iterace = 2      s = 0.165028

y={0., 0.00740444, 0.0166366, 0.0297699, 0.0490619,
  0.0763262, 0.111957, 0.154499, 0.201408, 0.250389, 0.300107, 0.350033,
  0.400011, 0.450004, 0.500001, 0.550001, 0.6, 0.65, 0.700001, 0.750384, 1.}

iterace = 3      s = 0.177539

y={0., 0.00282452, 0.00635372, 0.0114549, 0.0193258, 0.0316135,
  0.0502947, 0.0770608, 0.112317, 0.154636, 0.201449, 0.250399, 0.300109,
  0.350033, 0.400011, 0.450004, 0.500001, 0.550001, 0.600013, 0.651691, 1.}

iterace = 4      s = 0.188841

y={0., 0.00105803, 0.00238049, 0.00429713, 0.00728257, 0.0120624,
  0.0197438, 0.0319115, 0.0505006, 0.0771859, 0.112378, 0.15466, 0.201456,
  0.2504, 0.30011, 0.350034, 0.400012, 0.450008, 0.500134, 0.556275, 1.}

iterace = 5      s = 0.195511

y={0., 0.000393889, 0.000886247, 0.00160012, 0.00271372, 0.00450434,
  0.0074146, 0.0121504, 0.0198061, 0.0319575, 0.0505333, 0.0772061, 0.112388,
  0.154664, 0.201457, 0.250402, 0.30012, 0.350122, 0.401127, 0.470412, 1.}

iterace = 6      s = 0.189665

y={0., 0.000146455, 0.000329524, 0.000594971, 0.00100915, 0.00167553,
  0.00276047, 0.00453401, 0.00743447, 0.0121651, 0.0198189, 0.0319706, 0.0505491,
  0.0772292, 0.112431, 0.154766, 0.201773, 0.251703, 0.307437, 0.406285, 1.}

iterace = 7      s = 0.155175

y={0., 0.0000555323, 0.000124948, 0.0002256, 0.000382651, 0.000635362,
  0.0010469, 0.00172008, 0.00282295, 0.00463008, 0.00758828, 0.0124158, 0.0202321,
  0.0326625, 0.0517447, 0.0794279, 0.116939, 0.165636, 0.234036, 0.373375, 1.}

iterace = 8      s = 0.0753367

y={0., 0.0000285746, 0.0000642929, 0.000116084, 0.000196897, 0.000326934,
  0.000538703, 0.000885147, 0.00145287, 0.00238376, 0.00391041, 0.00641383, 0.0105171,
  0.0172344, 0.0281986, 0.0459917, 0.0746592, 0.121036, 0.200252, 0.363815, 1.}

iterace = 9      s = 0.0104333

```

```

y={0., 0.0000256221, 0.0000576498, 0.00010409, 0.000176553, 0.000293153,
  0.000483043, 0.000793693, 0.00130277, 0.00213755, 0.00350675, 0.00575281, 0.00943783,
  0.0154857, 0.0254198, 0.0417748, 0.0688698, 0.114543, 0.195458, 0.362762, 1.}

iterace = 10      s = 0.000147365

y={0., 0.0000255857, 0.0000575677, 0.000103942, 0.000176301, 0.000292736,
  0.000482355, 0.000792563, 0.00130091, 0.0021345, 0.00350176, 0.00574463, 0.00942445,
  0.0154639, 0.0253847, 0.04172, 0.0687906, 0.114448, 0.195385, 0.362748, 1.}

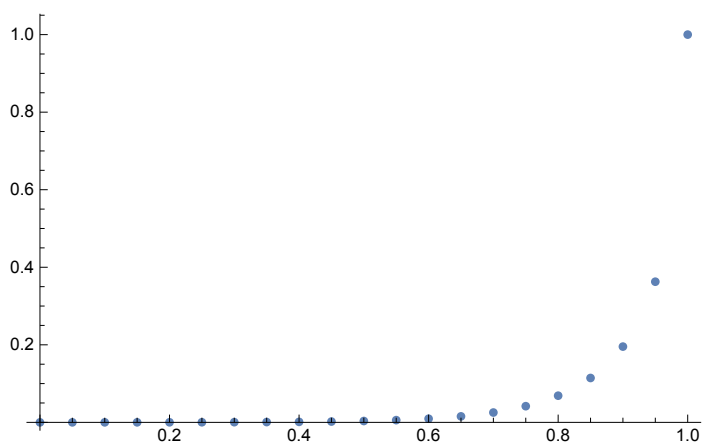
iterace = 11      s = 2.96088×10-8

y={0., 0.0000255856, 0.0000575677, 0.000103942, 0.000176301, 0.000292736,
  0.000482355, 0.000792562, 0.00130091, 0.0021345, 0.00350175, 0.00574463, 0.00942444,
  0.0154639, 0.0253847, 0.04172, 0.0687906, 0.114448, 0.195385, 0.362748, 1.}

```

Graf řešení $y(x)$

ListPlot[yres, PlotRange → All]



Tabulka řešení $y(x)$

MatrixForm[yres]

0.	0.
0.05	0.0000255856
0.1	0.0000575677
0.15	0.000103942
0.2	0.000176301
0.25	0.000292736
0.3	0.000482355
0.35	0.000792562
0.4	0.00130091
0.45	0.0021345
0.5	0.00350175
0.55	0.00574463
0.6	0.00942444
0.65	0.0154639
0.7	0.0253847
0.75	0.04172
0.8	0.0687906
0.85	0.114448
0.9	0.195385
0.95	0.362748
1.	1.

$\alpha = 20.0$

Definice parametrů diferenciální rovnice

$\alpha = 20.0;$

Definice pravé strany diferenciální rovnice

$f[x_, y1_, y2_] = \alpha \sinh[\alpha y1];$

Parametry programu DESite2

$a = 0.0;$

$b = 1.0;$

$\alpha 1 = 1;$

$\alpha 2 = 1;$

$\beta 1 = 0;$

$\beta 2 = 0;$

$\gamma 1 = 0;$

$\gamma 2 = 1;$

$\epsilon = 0.000001;$

$n = 20;$

$y0 = \text{Table}[(0.05 * (i - 1))^5, \{i, 1, n + 1\}]$

$\{0., 3.125 \times 10^{-7}, 0.00001, 0.0000759375, 0.00032, 0.000976563,$
 $0.00243, 0.00525219, 0.01024, 0.0184528, 0.03125, 0.0503284, 0.07776,$
 $0.116029, 0.16807, 0.237305, 0.32768, 0.443705, 0.59049, 0.773781, 1.\}$

$yres = \text{DESite2}[n, f, a, b, \alpha 1, \alpha 2, \beta 1, \beta 2, \gamma 1, \gamma 2, \epsilon, y0, 20];$

iterace = 0

$y = \{0., 3.125 \times 10^{-7}, 0.00001, 0.0000759375, 0.00032, 0.000976563,$
 $0.00243, 0.00525219, 0.01024, 0.0184528, 0.03125, 0.0503284, 0.07776,$
 $0.116029, 0.16807, 0.237305, 0.32768, 0.443705, 0.59049, 0.773781, 1.\}$

iterace = 1 $s = 0.0931029$

$y = \{0., 1.35252 \times 10^{-6}, 4.05755 \times 10^{-6}, 0.0000108201, 0.0000284028, 0.0000743844,$
 $0.00019464, 0.000507853, 0.00131238, 0.00331315, 0.00800604, 0.01809, 0.0374457,$
 $0.0702025, 0.119499, 0.187692, 0.277754, 0.393714, 0.540491, 0.723781, 1.\}$

iterace = 2 $s = 0.0880597$

$y = \{0., 3.26995 \times 10^{-7}, 9.80984 \times 10^{-7}, 2.61596 \times 10^{-6}, 6.86689 \times 10^{-6}, 0.0000179847,$
 $0.0000470872, 0.000123276, 0.00032273, 0.000844725, 0.00220845, 0.00574039,$
 $0.0145928, 0.034924, 0.0747536, 0.138913, 0.227962, 0.343738, 0.490492, 0.673781, 1.\}$

iterace = 3 $s = 0.0846417$

$y = \{0., 1.36996 \times 10^{-7}, 4.10987 \times 10^{-7}, 1.09596 \times 10^{-6}, 2.87691 \times 10^{-6}, 7.53475 \times 10^{-6}, 0.0000197274,$
 $0.0000516473, 0.000135214, 0.000353994, 0.000926739, 0.00242569, 0.00634108,$
 $0.0164517, 0.0412314, 0.0933898, 0.178601, 0.293803, 0.440496, 0.623782, 1.\}$

iterace = 4 $s = 0.0818337$

$y = \{0., 7.17513 \times 10^{-8}, 2.15254 \times 10^{-7}, 5.74011 \times 10^{-7}, 1.50678 \times 10^{-6}, 3.94632 \times 10^{-6}, 0.0000103322,$
 $0.0000270503, 0.0000708186, 0.000185405, 0.000485396, 0.00127076, 0.00332648,$
 $0.00870141, 0.0226529, 0.0574087, 0.130903, 0.243991, 0.390507, 0.573784, 1.\}$

iterace = 5 $s = 0.079164$

$y = \{0., 4.24546 \times 10^{-8}, 1.27364 \times 10^{-7}, 3.39637 \times 10^{-7}, 8.91547 \times 10^{-7}, 2.335 \times 10^{-6}, 6.11347 \times 10^{-6},$
 $0.0000160054, 0.0000419027, 0.000109703, 0.000287205, 0.000751912, 0.0019685,$
 $0.00515303, 0.0134807, 0.0351145, 0.0889523, 0.194609, 0.340537, 0.52379, 1.\}$

```

iterace = 6      s = 0.0762611
y={0., 2.71248×10-8, 8.13745×10-8, 2.16999×10-7, 5.69622×10-7, 1.49187×10-6, 3.90598×10-6,
  0.0000102261, 0.0000267722, 0.0000700906, 0.0001835, 0.000480408, 0.00125772,
  0.00329272, 0.00861966, 0.0225524, 0.0587689, 0.146916, 0.290624, 0.473809, 1.}

iterace = 7      s = 0.0732387
y={0., 1.83574×10-8, 5.50723×10-8, 1.46859×10-7, 3.85506×10-7, 1.00966×10-6, 2.64347×10-6,
  6.92075×10-6, 0.0000181188, 0.0000474356, 0.000124188, 0.000325128, 0.000851197,
  0.00222847, 0.00583428, 0.0152756, 0.0400123, 0.104741, 0.240905, 0.423869, 1.}

iterace = 8      s = 0.0692913
y={0., 1.28603×10-8, 3.85809×10-8, 1.02882×10-7, 2.70066×10-7, 7.07316×10-7, 1.85188×10-6,
  4.84833×10-6, 0.0000126931, 0.000033231, 0.0000869999, 0.000227769, 0.000596307,
  0.00156116, 0.00408723, 0.0107019, 0.0280421, 0.0737919, 0.191945, 0.374054, 1.}

iterace = 9      s = 0.0652374
y={0., 9.41684×10-9, 2.82505×10-8, 7.53347×10-8, 1.97754×10-7, 5.17926×10-7, 1.35602×10-6,
  3.55015×10-6, 9.29442×10-6, 0.0000243331, 0.0000637049, 0.000166782, 0.00043664,
  0.00114314, 0.00299283, 0.00783626, 0.0205319, 0.0540405, 0.145741, 0.324614, 1.}

iterace = 10     s = 0.0599219
y={0., 6.99669×10-9, 2.09901×10-8, 5.59735×10-8, 1.4693×10-7, 3.84818×10-7, 1.00752×10-6,
  2.63775×10-6, 6.90573×10-6, 0.0000180794, 0.0000473326, 0.000123918, 0.000324423,
  0.000849351, 0.00222365, 0.00582201, 0.0152497, 0.0400574, 0.107082, 0.276294, 1.}

iterace = 11     s = 0.0506483
y={0., 5.35301×10-9, 1.6059×10-8, 4.28241×10-8, 1.12413×10-7, 2.94416×10-7, 7.70834×10-7,
  2.01808×10-6, 5.28342×10-6, 0.0000138322, 0.0000362131, 0.0000948072, 0.000248208,
  0.000649819, 0.00170126, 0.00445418, 0.0116652, 0.0306108, 0.0813947, 0.231225, 1.}

iterace = 12     s = 0.0385367
y={0., 4.43521×10-9, 1.33056×10-8, 3.54816×10-8, 9.31393×10-8, 2.43936×10-7, 6.3867×10-7,
  1.67207×10-6, 4.37755×10-6, 0.0000114606, 0.0000300042, 0.0000785519, 0.000205652,
  0.000538404, 0.00140957, 0.00369046, 0.00966467, 0.025355, 0.0673325, 0.194539, 1.}

iterace = 13     s = 0.0216443
y={0., 3.98961×10-9, 1.19688×10-8, 3.19168×10-8, 8.37817×10-8, 2.19428×10-7, 5.74503×10-7,
  1.50408×10-6, 3.93774×10-6, 0.0000103091, 0.0000269897, 0.0000706599, 0.00018499,
  0.000484311, 0.00126795, 0.00331967, 0.00869339, 0.0228026, 0.0604799, 0.173704, 1.}

iterace = 14     s = 0.00544727
y={0., 3.87581×10-9, 1.16274×10-8, 3.10065×10-8, 8.13921×10-8, 2.1317×10-7, 5.58117×10-7,
  1.46118×10-6, 3.82543×10-6, 0.0000100151, 0.0000262199, 0.0000686445, 0.000179714,
  0.000470497, 0.00123178, 0.00322498, 0.00844539, 0.0221513, 0.0587383, 0.168492, 1.}

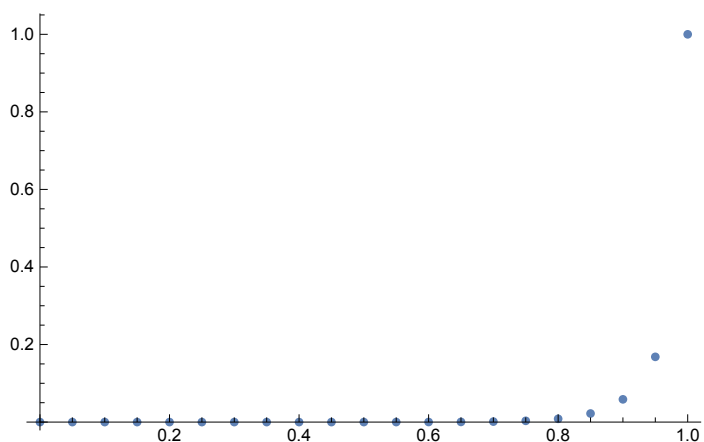
iterace = 15     s = 0.000274173
y={0., 3.86988×10-9, 1.16096×10-8, 3.0959×10-8, 8.12675×10-8, 2.12843×10-7, 5.57263×10-7,
  1.45894×10-6, 3.81957×10-6, 9.99977×10-6, 0.0000261797, 0.0000685394, 0.000179439,
  0.000469777, 0.0012299, 0.00322004, 0.00843246, 0.0221174, 0.058648, 0.168231, 1.}

iterace = 16     s = 6.44607×10-7
y={0., 3.86987×10-9, 1.16096×10-8, 3.09589×10-8, 8.12672×10-8, 2.12843×10-7, 5.57261×10-7,
  1.45894×10-6, 3.81956×10-6, 9.99973×10-6, 0.0000261796, 0.0000685392, 0.000179438,
  0.000469775, 0.00122989, 0.00322003, 0.00843243, 0.0221173, 0.0586478, 0.16823, 1.}

```

Graf řešení $y(x)$

ListPlot[yres, PlotRange → All]



Tabulka řešení $y(x)$

MatrixForm[yres]

$$\begin{pmatrix} 0. & 0. \\ 0.05 & 3.86987 \times 10^{-9} \\ 0.1 & 1.16096 \times 10^{-8} \\ 0.15 & 3.09589 \times 10^{-8} \\ 0.2 & 8.12672 \times 10^{-8} \\ 0.25 & 2.12843 \times 10^{-7} \\ 0.3 & 5.57261 \times 10^{-7} \\ 0.35 & 1.45894 \times 10^{-6} \\ 0.4 & 3.81956 \times 10^{-6} \\ 0.45 & 9.99973 \times 10^{-6} \\ 0.5 & 0.0000261796 \\ 0.55 & 0.0000685392 \\ 0.6 & 0.000179438 \\ 0.65 & 0.000469775 \\ 0.7 & 0.00122989 \\ 0.75 & 0.00322003 \\ 0.8 & 0.00843243 \\ 0.85 & 0.0221173 \\ 0.9 & 0.0586478 \\ 0.95 & 0.16823 \\ 1. & 1. \end{pmatrix}$$