

```
In[1]:= Get[FileNameJoin[{NotebookDirectory[], "DeStrelba.wl"}]]
```

Aplikační příklad 3

Apl. příklad 3: Axiální sdílení hmoty a tepla v trubkovém reaktoru lze na základě difuzního modelu popsat soustavou dvou nelineárních diferenciálních rovnic, které po kombinaci a převedení do bezrozměrného tvaru poskytnou rovnici

$$\frac{1}{Pe} \frac{\partial^2 y}{\partial x^2} - \frac{\partial y}{\partial x} - p y^m T^{-m} e^{(K-\frac{R}{T})} = 0, \text{ kde } T = 1 - H(1-y)$$

$$y(0) = 1 + \frac{1}{Pe} \frac{\partial y}{\partial x}(0), \quad \frac{\partial y}{\partial x}(1) = 0.$$

Použijte parametry $Pe=10$, $p=0.6$, $K=14.1$, $R=10.85$, $m=1.0$, $H=0.1437$

Definice parametrů diferenciální rovnice

```
In[2]:= Pe = 10;  
p = 0.6;  
K = 14.1;  
R = 10.85;  
m = 1.0;  
H = 0.1437
```

```
Out[7]= 0.1437
```

Definice pravé strany diferenciální rovnice

```
In[8]:= f[x_, y1_, y2_] = y2;  
g[x_, y1_, y2_] =  
Pe * y2 + Pe * p * y1^m * (1 - H * (1 - y1)) ^ (-m) * Exp[K - R / (1 - H * (1 - y1))];
```

Parametry programu Strelba1/Strelba2

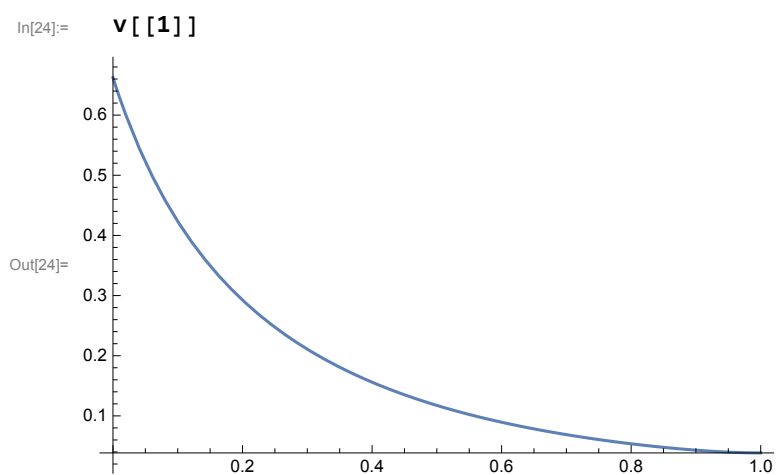
Poznámka: integrujeme od 1.0 do 0.0

```
In[10]:= a = 1.0;  
b = 0.0;  
α1 = 0;  
α2 = 1;  
β1 = 1;  
β2 = -1 / Pe;  
γ1 = 0;  
γ2 = 1;  
ε = 0.000001;  
h = 0.001;  
z0 = 0.05;  
m = 10;  
Lx = Table[N[a + i (b - a) / m], {i, 0, m}];
```

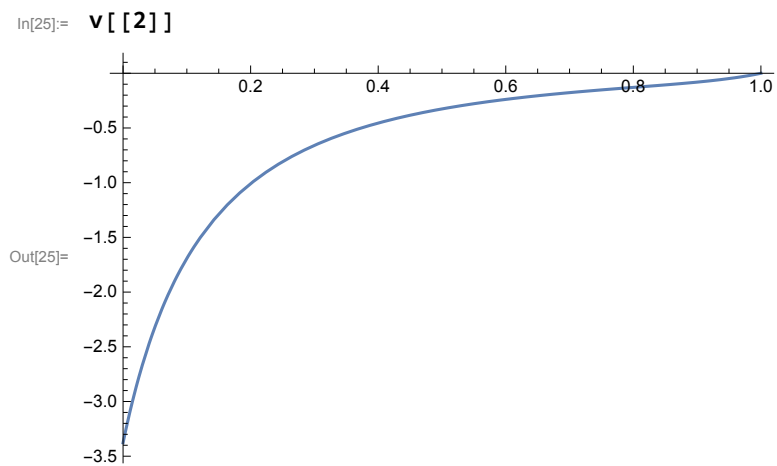
```
In[23]:= v = Strelba1[f, g, a, b, α1, α2, β1, β2, γ1, γ2, ε, h, z0, Lx];
```

i	z	s
0	0.05	
1	0.0445567	0.00544325
2	0.0402508	0.0043059
3	0.0386401	0.00161076
4	0.0384385	0.000201607
5	0.0384284	0.0000101114
6	0.0384279	4.19034×10^{-7}

Graf řešení $u_1(x)$



Graf řešení $u_2(x)$



Tabulka řešení $u_1(x)$

In[26]:= **MatrixForm**[v[[3]]]

Out[26]//MatrixForm=

$$\begin{pmatrix} 1. & 0.0384279 \\ 0.9 & 0.0430035 \\ 0.8 & 0.0535852 \\ 0.7 & 0.068813 \\ 0.6 & 0.089435 \\ 0.5 & 0.117386 \\ 0.4 & 0.15597 \\ 0.3 & 0.210847 \\ 0.2 & 0.292532 \\ 0.1 & 0.423337 \\ 0. & 0.662251 \end{pmatrix}$$

Tabulka řešení $u_2(x)$

In[27]:= **MatrixForm**[v[[4]]]

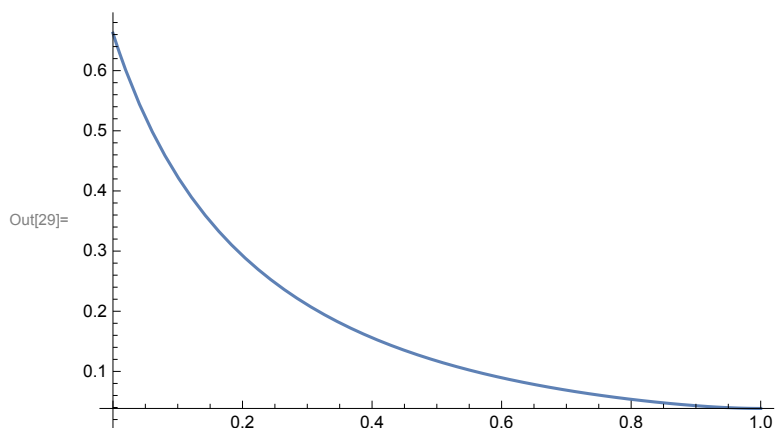
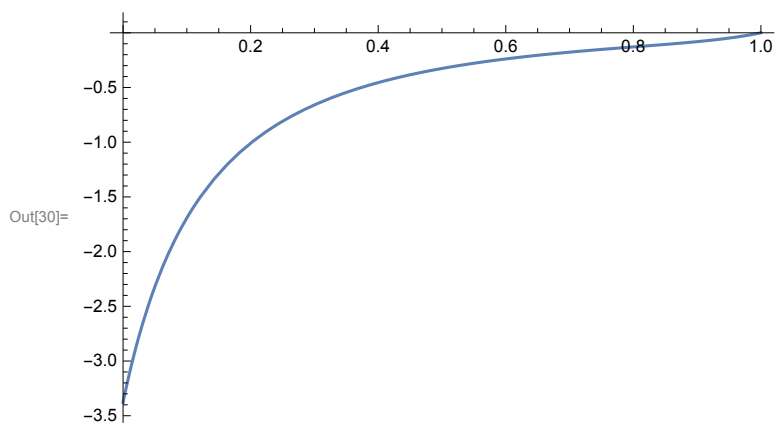
Out[27]//MatrixForm=

$$\begin{pmatrix} 1. & 0. \\ 0.9 & -0.0809329 \\ 0.8 & -0.128971 \\ 0.7 & -0.176948 \\ 0.6 & -0.238681 \\ 0.5 & -0.325695 \\ 0.4 & -0.455057 \\ 0.3 & -0.659059 \\ 0.2 & -1.00877 \\ 0.1 & -1.69215 \\ 0. & -3.3775 \end{pmatrix}$$

In[28]:= **v = Strelba2**[f, g, a, b, α_1 , α_2 , β_1 , β_2 , γ_1 , γ_2 , ϵ , z0, Lx];

i	z	s
0	0.05	
1	0.0440663	0.00593369
2	0.039751	0.00431528
3	0.0384999	0.00125115
4	0.0384281	0.0000717335
5	0.0384279	2.11861×10^{-7}

Graf řešení $u_1(x)$

In[29]:= **v[[1]]**Graf řešení $u_2(x)$ In[30]:= **v[[2]]**Tabulka řešení $u_1(x)$ In[31]:= **MatrixForm[v[[3]]]**

Out[31]//MatrixForm=

$$\begin{pmatrix} 1. & 0.0384279 \\ 0.9 & 0.0430035 \\ 0.8 & 0.0535852 \\ 0.7 & 0.068813 \\ 0.6 & 0.0894349 \\ 0.5 & 0.117386 \\ 0.4 & 0.15597 \\ 0.3 & 0.210847 \\ 0.2 & 0.292532 \\ 0.1 & 0.423337 \\ 0. & 0.662251 \end{pmatrix}$$
Tabulka řešení $u_2(x)$

```
In[32]:= MatrixForm[v[[4]]]
```

```
Out[32]//MatrixForm=
```

$$\begin{pmatrix} 1. & 0. \\ 0.9 & -0.0809329 \\ 0.8 & -0.128971 \\ 0.7 & -0.176948 \\ 0.6 & -0.238681 \\ 0.5 & -0.325695 \\ 0.4 & -0.455057 \\ 0.3 & -0.659059 \\ 0.2 & -1.00877 \\ 0.1 & -1.69215 \\ 0. & -3.37749 \end{pmatrix}$$